

The following is a complete listing of all claims in the application, with an indication of the status of each:

**Listing of claims:**

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- 1        1. (currently amended) A method of managing manufacturing logistics of end  
2        products comprising the steps of:  
3                maintaining an inventory of components, which components, termed  
4        “building blocks”, are built to stock, each said component having a cost;  
5                configuring-to-order end products using said components;  
6                establishing a base-stock level for each of said components; and  
7                replenishing said components from suppliers ~~following a base-stock~~  
8        ~~policy that establishes a base-stock level for each of said components that~~  
9        ~~minimizes in accordance with said base-stock levels so as to reduce a total~~  
10       ~~cost of inventory of said components,~~  
11               wherein said cost of at least one component differs from said cost of at  
12       least one other component.
- 1        2. (original) The method of managing manufacturing logistics of end  
2        products recited in claim 1, wherein the end products are personal computers  
3        (PCs) and the components are stock computer components.
- 1        3. (original) The method of managing manufacturing logistics of end  
2        products recited in claim 1, wherein the base-stock levels are derived from a  
3        greedy algorithm which iteratively reduces inventory budget until a budget  
4        constraint is satisfied.

1 4. (currently amended) A computer implemented process of managing  
 2 manufacturing logistics of configure-to-order end products comprising the  
 3 steps of:

4 a) initializing a process of managing manufacturing logistics of  
 5 configure-to-order end products by setting  $x_i := 0$  for each  $i \in S$ , setting  $r_{mi} :=$   
 6  $P(X_{mi} > 0)$ , setting  $\beta_m := 0$  for each  $m \in M$ , and setting  $\beta := 0$ , where  $S$  is a set  
 7 of components indexed by  $i$ ,  $M$  is a set of end products indexed by  $m$ ,  $x_i$  is a  
 8 probability of no-stockout of a component of index  $i$ ,  $r_{mi}$  is a probability that  
 9 a positive number of units of component  $i$  is used in the assembly of an end  
 10 product indexed by  $m$ ,  $\beta_m$  is a probability of stockout of an end product of  
 11 index  $m$ , and  $\beta$  is an upper limit on the stockout probability over all end  
 12 products;

13 b) setting a set of active components to  $A := \{\}$ ;

14 c) considering each  $i \in S$ , followed by considering each end product  $m$   
 15 that uses component  $i$  in its bill-of-material;

16 d) setting  $\beta_m := \beta_m + r_{mi} \Delta$ , for all  $m$  such that  $i \in S_m$  where  $\Delta$  is a unit  
 17 step size;

18 e) computing the a difference  $\delta_i := \max_m \{\beta_m\} - \beta$ ;

19 f) determining if  $\delta_i \leq 0$ , and if so, then adding component index  $i$  to the  
 20 set of active components,  $A := A + \{i\}$ ;

21 g) determining if the set of active components is non-empty, and if so,  
 22 then setting  $B := A$ , otherwise setting  $B := S$  where  $B$  is a set of component  
 23 indexes;

24 h) finding  $i^* := \arg \max_{i \in B} \{-c_i \sigma_i / r_{mi} g'(x_i + \Delta/2)\}$ , where  $-g'(\bullet)$  follows

25 the equation  $-g'(x) = -\Phi(\bar{\Phi}^{-1}(x)) \cdot \frac{-1}{\phi(\bar{\Phi}^{-1}(x))} = \frac{1-x}{\phi(\bar{\Phi}^{-1}(x))}$ , where  $\Phi(\cdot)$  is a

26 probability distribution function of the standard normal variate, and  $\phi(\cdot)$  is a  
 27 probability density function of the standard normal variate;

28 i) setting  $x_i^* := x_i^* + \Delta$  to update the probability of no-stockout of  
 29 component  $i^*$ ;

30 j) computing  $\beta := \max_{m \in M} \beta_m$ , and checking whether inequality  
 31  $\sum_{i \in S} c_i \sigma g(x_i) \leq B$ , where  $B$  is the budget limit on the expected overall

32 inventory cost, is satisfied and if so, stop and replenish components identified  
 33 by said set  $B$  from suppliers following a base-stock policy that minimizes a  
 34 total cost of inventory of said components  $i$ .

35 wherein said cost  $c_i$  of at least one component differs from said cost  
 36  $c_i$  of at least one other component ;

37 k) otherwise, updating  $\beta_m$  and for each  $m \in M_{i^*}$ , set  $\beta_m := \beta_m + r_{mi} \Delta$ , and  
 38 going to step b).

1 5. (currently amended) A system for managing manufacturing logistics of  
 2 end products comprising:  
 3 means for maintaining an inventory of components, which  
 4 components, termed "building blocks", are built to stock, each said component  
 5 having a cost;

6 means for configuring-to-order end products using said components;  
 7 means for establishing a base-stock level for each of said components;

8 and

9 means for replenishing said components from suppliers ~~following a~~  
 10 ~~base-stock policy that establishes a base-stock level for each of said~~  
 11 ~~components that minimizes in accordance with said base-stock levels so as to~~  
 12 reduce a total cost of inventory of said components.

13 wherein said cost of at least one component differs from said cost of at  
14 least one other component.

1        6. (original) The system for managing manufacturing logistics of end  
2        products recited in claim 5, wherein the end products are personal computers  
3        (PCs) and the components are stock computer components.

7. (original) The system for managing manufacturing logistics of end products recited in claim 5, wherein the base-stock levels are derived from a greedy algorithm which is iteratively computed by a processing unit to reduce inventory budget until a budget constraint is satisfied.

8. (currently amended) A method that translates end-product demand forecast in an assemble-to-order (ATO) environment into a forecast for components, taking into account outbound leadtime comprising the steps of:

defining in an assemble-to-order (ATO) environment an end product demand  $D_m(t)$  of type  $m$  in period  $t$ , each unit of type  $m$  demand requiring a subset of components, denoted  $S_m \subseteq S$ , as

$$D_i(t) = \sum_{m \in M_i} D_m(t + L_m^{\text{out}}); \text{ [and]}$$

8 deriving mean and variance for component demand  $D_i(t)$  as

$$9 \quad \mathbb{E}[D_i(t)] = \sum_{m \in M_i} \sum_l \mathbb{E}[D_m(t+l)] \mathbb{P}[L_m^{\text{out}}=l], \text{ and}$$

10 
$$\text{Var}[D_i(t)] = \sum_{m \in M_i} \sum_t E[D_m^2(t+\ell)] P[L_m^{\text{out}} = \ell] - \sum_{m \in M_i} \left( \sum_t E[D_m(t+\ell)] P[L_m^{\text{out}} = \ell] \right)^2, \text{ respectively; and}$$

11 replenishing said components from suppliers following a base stock  
 12 policy that minimizes a total cost of inventory of said components, each said  
 13 component having a cost,  
 14 wherein said cost of at least one component differs from said cost of at  
 15 least one other component.

1 9. (original) The method recited in claim 8, wherein the ATO environment is  
 2 extended to a configure-to-order (CTO) environment for stationary demand,  
 3 taking into account batch sizes comprising the steps of:  
 4 translating end-product demand into demand for each component  $i$  (per  
 5 period) as

6 
$$D_i = \sum_{m \in M_i} \sum_{k=1}^{D_m} X_{mi}(k).$$

7 where  $X_{mi}(k)$ , for  $k = 1, 2, \dots$ , are independent, identically distributed (i.i.d.)  
 8 copies of  $X_{mi}$ ;  
 9 deriving marginal distributions, and then the mean and the variance of  
 10  $X_{mi}$  as

11 
$$E[D_i] = \sum_{m \in M_i} E[X_{mi}] E[D_m], \text{ and}$$

$$\begin{aligned}
\text{Var}[D_i] &= \sum_{m \in M_i} \left( E[D_m] \text{Var}[X_{mi}] + \text{Var}[D_m] E^2[X_{mi}] \right) \\
&= \sum_{m \in M_i} \left( E^2[X_{mi}] E[D_m^2] + \text{Var}[X_{mi}] E[D_m] - E^2[X_{mi}] E^2[D_m] \right), \text{ respectively.}
\end{aligned}$$

10. (original) The method recited in claim 9, extended to non-stationary demand, wherein the mean and the variance of  $X_{mi}$  are generalized as

$$E[D_i(t)] = \sum_{m \in M_i} E[X_{mi}] \sum_t E[D_m(t+\ell)] P[L_m^{\text{out}} = \ell], \text{ and}$$

$$\begin{aligned}
\text{Var}[D_i(t)] &= \sum_{m \in M_i} E^2(X_{mi}) \sum_t E[D_m^2(t+\ell)] P[L_m^{\text{out}} = \ell] \\
&\quad + \sum_{m \in M_i} \text{Var}(X_{mi}) \sum_t E[D_m(t+\ell)] P[L_m^{\text{out}} = \ell] \\
&\quad - \sum_{m \in M_i} E^2(X_{mi}) \left( \sum_t E[D_m(t+\ell)] P[L_m^{\text{out}} = \ell] \right)^2, \text{ respectively.}
\end{aligned}$$

11. (currently amended) The method recited in claim 9, further comprising the steps of:

defining  $R_i(t)$  as a reorder point (or, base-stock level) in period  $t$  as

$$R_i(t) := \mu_i(t) + k_i(t) \sigma_i(t),$$

where  $k_i(t)$  is ~~the~~ a desired safety factor, while  $\mu_i(t)$  and  $\sigma_i(t)$  can be derived (via queuing analysis) as

7 
$$\mu_i(t) = \sum_{s=t}^{t+\ell_i^{\text{in}}-1} E[D_i(s)], \text{ and}$$

8 
$$\sigma_i^2(t) = \sum_{s=t}^{t+\ell_i^{\text{in}}-1} \text{Var}[D_i(s)], \text{ respectively,}$$

9 where  $\ell_i^{\text{in}} := E[L_i^{\text{in}}]$  is expected in-bound leadtime; and

10 translating  $R_i(t)$  into “days of supply” (DOS), where the  $\mu_i(t)$  part of  
 11  $R_i(t)$  translates into periods of demand and the  $k_i(t)\sigma_i(t)$  part of  $R_i(t)$  is turned  
 12 into

13 
$$\frac{\frac{k_i(t)\sigma_i(t)}{\mu_i(t)}}{\ell_i^{\text{in}}}$$

14 periods of demand so that  $R_i(t)$  is expressed in terms of periods of DOS as

15 
$$\text{DOS}_i(t) = \ell_i^{\text{in}} \left[ 1 + k_i(t) \frac{\sigma_i(t)}{\mu_i(t)} \right].$$

1 12. (original) The method recited in claim 11, wherein demand is stationary  
 2 in which for each demand class  $m$ ,  $D_m(t)$  is invariant in distribution over time,  
 3 so that the mean and the variance of demand per period for each component  $i$   
 4 reduce to

5  $\mu_i = \ell_i^{\text{in}} E[D_i]$ , and  $\sigma_i^2 = \ell_i^{\text{in}} \text{Var}[D_i]$ , respectively, and

6  $R_i = \ell_i^{\text{in}} E[D_i] + k_i \sqrt{\ell_i^{\text{in}}} \text{sd}[D_i]$ , and hence,

7 
$$\text{DOS}_i = \frac{R_i}{E[D_i]} = \ell_i^{\text{in}} + k_i \theta_i \sqrt{\ell_i^{\text{in}}} = \ell_i^{\text{in}} \left[ 1 + k_i \frac{\theta_i}{\sqrt{\ell_i^{\text{in}}}} \right],$$

8 where  $\theta_i := \text{sd}[D_i]/E[D_i]$  is the coefficient of variation of the demand *per*  
 9 *period* for component  $i$ , and hence  $\theta_i / \sqrt{\ell_i^{\text{in}}}$  is the coefficient of variation of the  
 10 demand over the leadtime  $\ell_i^{\text{in}}$ .

1 13. (currently amended) A method that relates service requirements to  
 2 base-stock levels of components in an assemble-to-order (ATO) environment  
 3 comprising the steps of:

4 defining in an assemble-to-order (ATO) environment each order of  
 5 type  $m$  as requiring exactly one unit of component  $i \in S_m$ ,  $\alpha$  as a required  
 6 service level, referred to as off-shelf availability of all the components  
 7 required to configure a unit of type  $m$  product, for any  $m$ , and  $E_i$  as an event  
 8 that component  $i$  is out of stock;

9 determining a probability  $P$  for each end product  $m \in M$ ,

10 
$$P[\cup_{i \in S_m} E_i] \leq 1 - \alpha, \text{ and}$$



$$11 \quad P[\cup_{i \in S_m} E_i] = \sum_i P(E_i) - \sum_{i < j} P(E_i \cap E_j) + \sum_{i < j < k} P(E_i \cap E_j \cap E_k) - \dots, \text{ and}$$

$$12 \quad P[\cup_{i \in S_m} E_i] \approx \sum_{i \in S_m} P(E_i) = \sum_{i \in S_m} \bar{\Phi}(k_i) \leq 1 - \alpha; \text{ and}$$

13 establishing base stock levels for each component  $i$  that minimize a  
 14 total cost of inventory of said components, each said component having a cost,  
 15 wherein said cost of at least one component differs from said cost of at  
 16 least one other component.

1 14. (previously presented) The method recited in 13, wherein the method is  
 2 extended to a configure-to-order (CTO) environment taking into account batch  
 3 sizes, further comprising the steps of:

4 defining  $A \subseteq S_m$  as a certain configuration, which occurs in a demand  
 5 stream with probability  $P(A)$ ;

6 weighting a no-stockout probability,  $\prod_{i \in A} \Phi(k_i)$ , by  $P(A)$ ;

7 changing the service requirement to

$$\begin{aligned} \alpha &\leq \sum_{A \subseteq S_m} P(A) \prod_{i \in A} \Phi(k_i) \\ &\approx \sum_{A \subseteq S_m} P(A) [1 - \sum_{i \in A} \bar{\Phi}(k_i)] \\ 8 \quad &= 1 - \sum_{A \subseteq S_m} P(A) \sum_{i \in A} \bar{\Phi}(k_i) \\ &= 1 - \sum_{i \in S_m} \left( \sum_{A \ni i} P(A) \right) \bar{\Phi}(k_i); \text{ and} \end{aligned}$$

9 extending the CTO environment the service requirement to

10 
$$\sum_{i \in S_m} r_{mi} \bar{\Phi}(k_i) \leq 1 - \alpha$$

11 where  $r_{mi}$  is the probability that a positive number of units of component  $i$  is  
 12 used in the assembly of an end product indexed by  $m$ .

1 15. (currently amended) A method that translates service requirements in  
 2 terms of leadtimes into requirements for off-shelf availability of components  
 3 comprising the steps of:

4 relating an off-shelf availability requirement to standard customer  
 5 service requirements expressed in terms of leadtimes,  $W_m$ , where a required  
 6 service level of type  $m$  demand is

7 
$$P[W_m \leq w_m] \geq \alpha, \quad m \in M,$$

8 where  $w_m$ 's are given data and  $P$  is probability;

9 when there is no stockout at any store  $i \in S_m$ , denoting the associated  
 10 probability as  $\pi_{0m}(t)$ , a delay being  $L_i^{\text{out}}$ , the out-bound leadtime;

11 when there is a stockout at one or several stores in the subset  $s \subseteq S_m$ ,  
 12 denoting the associated probability as  $\pi_{sm}(t)$ , so that the delay becomes  
 13  $L_i^{\text{out}} + \tau_s$ , where  $\tau_s$  is the additional delay before the missing components in  $s$   
 14 become available;

15 determining  $P[W_m \leq w_m] = \pi_{0m}(t)P[L_m^{\text{out}} \leq w_m] + \sum_{s \in S_m} \pi_{sm}(t)P[L_m^{\text{out}} + \tau_s \leq w_m];$

16 assuming that

17  $L_m^{\text{out}} \leq w_m$  and  $L_m^{\text{out}} + \tau_s > w_m$

18 both hold *almost surely*, so that when the (nominal) outbound leadtime is  
19 nearly deterministic and shorter than what customers require, whereas the  
20 replenish leadtime for any component is substantially longer; and

21 replenishing said components from suppliers following a base stock  
22 policy that minimizes a total cost of inventory of said components, each said  
23 component having a cost,

24 wherein said cost of at least one component differs from said cost of at  
25 least one other component.

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